

## NEURAL NETWORK-BASED ADAPTIVE COMMAND FILTERED POSITION TRACKING CONTROL FOR INDUCTION MOTORS

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**ABSTRACT.** *This paper developed an adaptive neural networks (NNs) command filtered position tracking control approach for induction motors. Neural networks are used to approximate unknown nonlinear functions and the adaptive command filtered backstepping is employed to construct controllers. Therefore, the proposed control method can overcome the problems of “nonlinear systems with parameter uncertainties” and “explosion of complexity” inherent in the traditional backstepping design and the adaptive neural controllers guarantee the tracking error can converge to a small neighborhood of the origin. Then, simulation results illustrate the effectiveness of the proposed approach.*

**Keywords:** Induction motor, Neural networks, Command filtered control, Backstepping

**1. Introduction.** In the past decades, induction motors (IMs) have been widely used in industrial applications because of their simple and robust construction, low cost, high reliability and ruggedness. However, the control of IMs is complex due to its highly nonlinear, multivariable dynamic model. Hence, many control techniques have been developed to control IMs, such as sliding mode control [1], backstepping control [2] and other control methods [3]. Backstepping control is considered to be a powerful tool for the design of controllers for nonlinear systems. However, there are some drawbacks in backstepping approach. One problem is that certain functions must be linear in the unknown system parameters. Another limitation is the “explosion of complexity” caused by the repeated differentiations of virtual input. To overcome these problems, a command filtered backstepping technique is proposed to approximate the derivative of the virtual control by utilizing the output of a command filter at each step of the adaptive backstepping approach [4]. In addition, NN approximation method has been used in many applications, mainly by its inherent capability for modeling and controlling highly uncertain, nonlinear and complex systems [5]. Therefore, NNs can be employed to control the systems which are too complex to have a precise mathematical model.

Motivated by the above observations, NN approximation-based command filtered adaptive backstepping control is proposed for the IMs system in this paper. Compared with the traditional control methods, the benefits of the presented approach include: 1) The command filtered control technique is proposed to overcome the problem of “explosion of complexity”; 2) NNs are used to approximate the unknown nonlinear functions to solve the problem of the unknown system parameters; 3) The proposed method in this paper only needs the information of the desired trajectory and its first derivative, which makes it more suitable for practical applications where higher order derivations of the desired trajectory cannot be obtained. It is proved that the proposed approach can guarantee that the tracking error can converge to a small range of the origin and all the closed-loop signals are bounded. Simulation results illustrate the effectiveness of the proposed approach. The rest of the paper is organized as follows. Section 2 describes the mathematical model

of the position drive system for induction motors. The command filtered neural adaptive backstepping controllers are designed in Section 3. In Section 4, the simulation results are given. Finally, some conclusions are presented.

**2. Mathematical Model of the IM Drive System.** Induction motor’s dynamic mathematical model can be described in the well-known ( $d$ - $q$ ) frame as follows [6]:

$$\begin{cases} \frac{d\Theta}{dt} = \omega \\ \frac{d\omega}{dt} = \frac{n_p L_m}{L_r J} \psi_d i_q - \frac{T_L}{J} \\ \frac{di_q}{dt} = -\frac{L_m^2 R_r + L_r^2 R_s}{\sigma L_s L_r^2} i_q - \frac{L_m n_p}{\sigma L_s L_r} \omega \psi_d - n_p \omega i_d - \frac{L_m R_r}{L_r} \frac{i_q i_d}{\psi_d} + \frac{1}{\sigma L_s} u_q \\ \frac{d\psi_d}{dt} = -\frac{R_r}{L_r} \psi_d + \frac{L_m R_r}{L_r} i_d \\ \frac{di_d}{dt} = -\frac{L_m^2 R_r + L_r^2 R_s}{\sigma L_s L_r^2} i_d + \frac{L_m R_r}{\sigma L_s L_r^2} \psi_d + n_p \omega i_q + \frac{L_m R_r}{L_r} \frac{i_q^2}{\psi_d} + \frac{1}{\sigma L_s} u_d \end{cases} \quad (1)$$

where  $\sigma = 1 - \frac{L_m^2}{L_s L_r}$ .  $\omega$ ,  $L_m$ ,  $n_p$ ,  $J$ ,  $T_L$  and  $\psi_d$  denote the rotor angular velocity, mutual inductance, pole pairs, inertia, load torque and rotor flux linkage, respectively.  $i_d$  and  $i_q$  stand for the  $d$ - $q$  axis currents.  $u_d$  and  $u_q$  are the  $d$ - $q$  axis voltages.  $R_s$  and  $L_s$  mean the resistance, inductance of the stator.  $R_r$  and  $L_r$  denote the resistance, inductance of the rotor. For simplicity, the following notations are introduced:  $x_1 = \Theta$ ,  $x_2 = \omega$ ,  $x_3 = i_q$ ,  $x_4 = \psi_d$ ,  $x_5 = i_d$ ,  $a_1 = \frac{n_p L_m}{L_r}$ ,  $b_1 = -\frac{L_m^2 R_r + L_r^2 R_s}{\sigma L_s L_r^2}$ ,  $b_2 = -\frac{n_p L_m}{\sigma L_s L_r}$ ,  $b_3 = n_p$ ,  $b_4 = \frac{L_m R_r}{L_r}$ ,  $b_5 = \frac{1}{\sigma L_s}$ ,  $c_1 = -\frac{R_r}{L_r}$ ,  $d_2 = \frac{L_m R_r}{\sigma L_s L_r^2}$ . By using these notations, the dynamic model of IM driver system can be described by the following differential equations:

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = \frac{a_1}{J} x_3 x_4 - \frac{T_L}{J} \\ \dot{x}_3 = b_1 x_3 + b_2 x_2 x_4 - b_3 x_2 x_5 - b_4 \frac{x_3 x_5}{x_4} + b_5 u_q \\ \dot{x}_4 = c_1 x_4 + b_4 x_5 \\ \dot{x}_5 = b_1 x_5 + d_2 x_4 + b_3 x_2 x_3 + b_4 \frac{x_3^2}{x_4} + b_5 u_d \end{cases} \quad (2)$$

In this paper, the radial basis function (RBF) neural network will be used to approximate the unknown continuous function  $\varphi(z) : R^q \rightarrow R$  as  $\hat{\varphi}(z) = \phi^{*T} P(z)$  where  $z \in \Omega_z \subset R^q$  is the input vector with  $q$  being the neural network input dimension,  $\phi^* = [\phi_1^*, \dots, \phi_n^*]^T \in R^n$  is the weight vector,  $P(z) = [p_1(z), \dots, p_n(z)]^T \in R^n$  is the basis function vector with  $n > 1$  being the neural network node number, and  $p_i(z)$  are chosen as the commonly used Gaussian function in the following form:  $p_i(z) = \exp\left[-\frac{(z-\nu_i)^T(z-\nu_i)}{q_i^2}\right]$ ,  $i = 1, 2, \dots, n$  where  $\nu_i = [\nu_{i1}, \dots, \nu_{iq}]^T$  is the center of the receptive field and  $q_i$  is the width of the Gaussian function. It has been proved in [7] that, for given scalar  $\varepsilon > 0$ , by choosing sufficiently large  $l$ , the RBF neural network can approximate any continuous function over a compact set  $\Omega_z \in R^q$  to arbitrary accuracy as  $\varphi(z) = \phi^T P(z) + \delta(z) \forall z \in \Omega_z \subset R^q$  where  $\delta(z)$  is the approximation error, satisfying  $|\delta(z)| \leq \varepsilon$  and  $\phi$  is an unknown ideal constant weight vector, which is an artificial quantity required for analytical purpose. Typically,  $\phi$  is chosen as the value of  $\phi^*$  that minimizes  $|\delta(z)|$  for all  $z \in \Omega_z$ .

**Lemma 2.1.** *The command filter [4] is defined as*

$$\begin{cases} \dot{\varphi}_1 = \omega_n \varphi_2 \\ \dot{\varphi}_2 = -2\zeta \omega_n \varphi_2 - \omega_n (\varphi_1 - \alpha_1) \end{cases} \quad (3)$$

If the input signal  $\alpha_1$  satisfies  $|\dot{\alpha}_1| \leq \rho_1$  and  $|\ddot{\alpha}_1| \leq \rho_2$  for all  $t \geq 0$ , where  $\rho_1$  and  $\rho_2$  are positive constants and  $\varphi_1(0) = \alpha_1(0)$ ,  $\varphi_2(0) = 0$ , then for any  $\mu > 0$ , there exist  $\omega_n > 0$  and  $\zeta \in (0, 1]$ , such that  $|\varphi_1 - \alpha_1| \leq \mu$ ,  $|\dot{\varphi}_1|$ ,  $|\ddot{\varphi}_1|$  and  $|\ddot{\varphi}_1|$  are bounded.

**3. Adaptive Neural Command Filtered Control for IMs.** In this section, we will present an adaptive neural command filtered control for IMs via backstepping. Design the tracking error variable as

$$z_1 = x_1 - x_{1d}, z_2 = x_2 - x_{1,c}, z_3 = x_3 - x_{2,c}, z_4 = x_4 - x_{4d}, z_5 = x_5 - x_{3,c} \quad (4)$$

where  $x_{1d}$  and  $x_{4d}$  are reference signals, the virtual controllers  $\alpha_1, \alpha_2$  and  $\alpha_3$  pass through the command filter and we will get  $x_{1,c}, x_{2,c}$  and  $x_{3,c}$  that will be constructed later.

**Step 1:** For the first equation of (2), consider Lyapunov function candidate as  $V_1 = \frac{1}{2}z_1^2$ , and the time derivative of  $V_1$  is computed by

$$\dot{V}_1 = z_1\dot{z}_1 = z_1(z_2 + x_{1,c} - \alpha_1 + \alpha_1 - \dot{x}_{1d}) \quad (5)$$

Construct the virtual control law  $\alpha_1$  as  $\alpha_1 = -k_1z_1 + \dot{x}_{1d}$ . Then (5) can be written as  $\dot{V}_1 = -k_1z_1^2 + z_1z_2 + z_1(x_{1,c} - \alpha_1)$ .

**Step 2:** Differentiating  $z_2$  we get  $\dot{z}_2 = \frac{a_1}{J}x_3x_4 - \frac{T_L}{J} - \dot{x}_{1,c}$ . Choose the Lyapunov function candidate as  $V_2 = V_1 + \frac{1}{2}z_2^2$ , and then we have  $\dot{V}_2 = \dot{V}_1 + z_2(a_1x_3x_4 - T_L - J\dot{x}_{1,c})$ . In this paper, due to the parameter  $T_L$  being bounded in practice system, we assume the  $T_L$  is unknown but its upper bound is  $d > 0$ . Namely,  $0 \leq T_L \leq d$ . Obviously,  $-z_2T_L \leq \frac{1}{2\varepsilon_1^2}z_2^2 + \frac{1}{2}\varepsilon_1^2d^2$ , where  $\varepsilon_1$  is an arbitrary small positive constant. Then we can get

$$\dot{V}_2 \leq \frac{1}{2}\varepsilon_1^2d^2 + z_2(x_3 + f_1) + \dot{V}_1 \quad (6)$$

where  $f_2(Z) = a_1x_3x_4 + \frac{1}{2\varepsilon_1^2}z_2 - x_3$ ,  $Z = [x_1, x_2, x_3, x_4, x_5]$ . According to the RBF neural network approximation property, for given  $\varepsilon_2 > 0$ , there exists an RBF NN  $\phi_2^T P_2(Z)$  such that  $f_2(Z) = \phi_2^T P_2(Z) + \delta_2(Z)$ , where  $\delta_2(Z)$  is the approximation error and satisfies  $|\delta_2| \leq \varepsilon_2$ . Consequently, a straightforward calculation produces the following inequality.

$$z_2f_2(Z) = z_2(\phi_2^T P_2(Z) + \delta_2(Z)) \leq \frac{1}{2l_2^2}z_2^2 \|\phi_2\|^2 P_2^T(Z)P_2(Z) + \frac{1}{2}l_2^2 + \frac{1}{2}z_2^2 + \frac{1}{2}\varepsilon_2^2 \quad (7)$$

Construct the virtual control law  $\alpha_2$  as  $\alpha_2 = -k_2z_2 - \frac{1}{2}z_2 - z_1 - \frac{1}{2l_2^2}z_2\hat{\theta}P_2^T P_2 + J\dot{x}_{1,c}$ , with  $k_2 > 0$  being a constant and  $\hat{\theta}$  is the estimation of the unknown constant  $\theta$  which will be specified later. Substituting (7) into (6), we can obtain

$$\begin{aligned} \dot{V}_2 \leq & -k_1z_1^2 - k_2z_2^2 + z_1(x_{1,c} - \alpha_1) + \frac{1}{2}\varepsilon_1^2d^2 + z_2(x_{2,c} - \alpha_2) \\ & + \frac{1}{2}l_2^2 + \frac{1}{2}\varepsilon_2^2 + \frac{1}{2l_2^2}z_2^2 \left( \|\phi_2\|^2 - \hat{\theta} \right) P_2^T P_2 + z_2z_3 \end{aligned} \quad (8)$$

**Step 3:** From the third equation of (2) and (3) we have  $\dot{z}_3 = \dot{x}_3 - \dot{x}_{2,c} = b_1x_3 + b_2x_2x_4 - b_3x_2x_5 - b_4\frac{x_3x_5}{x_4} + b_5u_q - \dot{x}_{2,c}$ . Now choose the Lyapunov function candidate as  $V_3 = V_2 + \frac{1}{2}z_3^2$ . Obviously, the time derivative of  $V_3$  is given by

$$\begin{aligned} \dot{V}_3 \leq & -k_1z_1^2 - k_2z_2^2 + z_1(x_{1,c} - \alpha_1) + \frac{1}{2}\varepsilon_1^2d^2 + z_2(x_{2,c} - \alpha_2) + \frac{1}{2}l_2^2 \\ & + \frac{1}{2}\varepsilon_2^2 + \frac{1}{2l_2^2}z_2^2 \left( \|\phi_2\|^2 - \hat{\theta} \right) P_2^T P_2 + z_2z_3 + z_3(f_3 + b_5u_q - \dot{x}_{2,c}) \end{aligned} \quad (9)$$

where  $f_3(Z) = b_1x_3 + b_2x_2x_4 - b_3x_2x_5 - b_4\frac{x_3x_5}{x_4} = \phi_3^T P_3(Z) + \delta_3(Z)$ . Similarly, for given  $\varepsilon_3 > 0$ , we can get

$$z_3f_3(Z) \leq \frac{1}{2l_3^2}z_3^2 \|\phi_3\|^2 P_3^T(Z)P_3(Z) + \frac{1}{2}l_3^2 + \frac{1}{2}z_3^2 + \frac{1}{2}\varepsilon_3^2 \quad (10)$$

The control law  $u_q$  is designed as  $u_q = \frac{1}{b_5} \left( -k_3 z_3 - \frac{1}{2} z_3 - z_2 + \dot{x}_{2,c} - \frac{1}{2l_3^2} z_3 \hat{\theta} P_3^T P_3 \right)$ . Substituting (10) and  $u_q$  into (9), we can obtain

$$\begin{aligned} \dot{V}_3 \leq & \sum_{i=1}^3 -k_i z_i^2 + z_1 (x_{1,c} - \alpha_1) + z_2 (x_{2,c} - \alpha_2) + \frac{1}{2} \varepsilon_1^2 d^2 + \frac{1}{2} l_2^2 + \frac{1}{2} \varepsilon_2^2 \\ & + \frac{1}{2} l_3^2 + \frac{1}{2} \varepsilon_3^2 + \frac{1}{2l_2^2} z_2^2 \left( \|\phi_2\|^2 - \hat{\theta} \right) P_2^T P_2 + \frac{1}{2l_3^2} z_3^2 \left( \|\phi_3\|^2 - \hat{\theta} \right) P_3^T P_3 \end{aligned} \quad (11)$$

**Step 4:** For the reference signal  $x_{3d}$ , one has  $\dot{z}_4 = \dot{x}_4 - \dot{x}_{4d}$ . Choose the Lyapunov candidate function as  $V_4 = V_3 + \frac{1}{2} z_4^2$ . Then the time derivative of  $V_4$  is given by

$$\begin{aligned} \dot{V}_4 \leq & \sum_{i=1}^3 -k_i z_i^2 + z_1 (x_{1,c} - \alpha_1) + z_2 (x_{2,c} - \alpha_1) + \frac{1}{2} \varepsilon_1^2 d^2 + \frac{1}{2} l_2^2 + \frac{1}{2} \varepsilon_2^2 + \frac{1}{2} l_3^2 \\ & + \frac{1}{2} \varepsilon_3^2 + \frac{1}{2l_2^2} z_2^2 \left( \|\phi_2\|^2 - \hat{\theta} \right) P_2^T P_2 + \frac{1}{2l_3^2} z_3^2 \left( \|\phi_3\|^2 - \hat{\theta} \right) P_3^T P_3 + z_4 (c_1 x_4 + b_4 x_5 - \dot{x}_{4d}) \end{aligned} \quad (12)$$

Construct the virtual control law  $\alpha_3$  as  $\alpha_3 = \frac{1}{b_4} (-k_4 z_4 + \dot{x}_{4d} - c_1 x_4)$ . Substituting  $\alpha_3$  into (12) results in  $\dot{V}_4 \leq \dot{V}_3 - k_4 z_4^2 + b_4 z_4 z_5 + b_4 z_4 (x_{3,c} - \alpha_3)$ .

**Step 5:** At this step, we will construct the control law  $u_d$ . Choose  $V_5 = V_4 + \frac{1}{2} z_5^2$ . Then, we have  $\dot{V}_5 = \dot{V}_4 + z_5 (f_5 + b_5 u_d - \dot{x}_{3,c})$ , where  $f_5(Z) = b_1 x_5 + d_2 x_4 + b_3 x_2 x_3 + b_4 \frac{x_3^2}{x_4} = \phi_5^T P_5(Z) + \delta_5(Z)$ . Similarly,

$$z_5 f_5(Z) \leq \frac{1}{2l_5^2} z_5^2 \|\phi_5\|^2 P_5^T(Z) P_5(Z) + \frac{1}{2} l_5^2 + \frac{1}{2} z_5^2 + \frac{1}{2} \varepsilon_5^2 \quad (13)$$

We design  $u_d$  as  $u_d = \frac{1}{b_5} \left( -k_5 z_5 - \frac{1}{2} z_5 - b_4 z_4 + \dot{x}_{3,c} - \frac{1}{2l_5^2} z_5 \hat{\theta} P_5^T P_5 \right)$ . Design  $\theta = \max\{\|\phi_2\|^2, \|\phi_3\|^2, \|\phi_5\|^2\}$ ,  $\tilde{\theta} = \hat{\theta} - \theta$ . Furthermore, it can be verified easily that

$$\begin{aligned} \dot{V}_5 \leq & - \sum_{i=1}^5 k_i z_i^2 + z_1 (x_{1,c} - \alpha_1) + z_2 (x_{2,c} - \alpha_2) + b_4 z_4 (x_{3,c} - \alpha_3) \\ & + \frac{1}{2} l_2^2 + \frac{1}{2} \varepsilon_2^2 + \frac{1}{2} l_3^2 + \frac{1}{2} \varepsilon_3^2 + \frac{1}{2} l_5^2 + \frac{1}{2} \varepsilon_5^2 \\ & + \frac{1}{2} \varepsilon_1^2 d^2 - \frac{1}{2l_2^2} z_2^2 \tilde{\theta} P_2^T P_2 - \frac{1}{2l_3^2} z_3^2 \tilde{\theta} P_3^T P_3 - \frac{1}{2l_5^2} z_5^2 \tilde{\theta} P_5^T P_5 \end{aligned} \quad (14)$$

Then we choose the Lyapunov function as  $V = V_5 + \frac{1}{2r_1} \tilde{\theta}^2$ . And the time derivative of  $V$  is given by

$$\begin{aligned} \dot{V} \leq & - \sum_{i=1}^5 k_i z_i^2 + z_1 (x_{1,c} - \alpha_1) + z_2 (x_{2,c} - \alpha_2) + b_4 z_4 (x_{3,c} - \alpha_3) \\ & + \frac{1}{2} l_2^2 + \frac{1}{2} \varepsilon_2^2 + \frac{1}{2} l_3^2 + \frac{1}{2} \varepsilon_3^2 + \frac{1}{2} l_5^2 + \frac{1}{2} \varepsilon_5^2 + \frac{1}{2} \varepsilon_1^2 d^2 \\ & + \frac{1}{r_1} \tilde{\theta} \left( \dot{\hat{\theta}} - \frac{r_1}{2l_2^2} z_2^2 P_2^T P_2 - \frac{r_1}{2l_3^2} z_3^2 P_3^T P_3 - \frac{r_1}{2l_5^2} z_5^2 P_5^T P_5 \right) \end{aligned} \quad (15)$$

We choose the adaptive law as

$$\dot{\hat{\theta}} = \frac{r_1}{2l_2^2} z_2^2 P_2^T P_2 + \frac{r_1}{2l_3^2} z_3^2 P_3^T P_3 + \frac{r_1}{2l_5^2} z_5^2 P_5^T P_5 - m_1 \hat{\theta} \quad (16)$$

where  $m_1$  and  $l_i$  for  $i = 2, 3, 5$  are positive constants.

**Proof:** To address the stability analysis of the resulting closed-loop system, substituting (16) into (15), we have

$$\begin{aligned} \dot{V} \leq & -\sum_{i=1}^5 k_i z_i^2 + \frac{1}{2}l_2^2 + \frac{1}{2}\varepsilon_2^2 + \frac{1}{2}l_3^2 + \frac{1}{2}\varepsilon_3^2 + \frac{1}{2}l_5^2 + \frac{1}{2}\varepsilon_5^2 + \frac{1}{2}\varepsilon_1^2 d^2 \\ & -\frac{m_1 \tilde{\theta} \hat{\theta}}{r_1} + z_1(x_{1,c} - \alpha_1) + z_2(x_{2,c} - \alpha_2) + b_4 z_4(x_{3,c} - \alpha_3) \end{aligned} \quad (17)$$

From  $|x_{i,c} - \alpha_i| < \mu$  and using the Young's inequalities, we can get  $z_1(x_{1,c} - \alpha_1) \leq z_1^2 + \frac{1}{4}\mu^2$ ,  $z_2(x_{2,c} - \alpha_2) \leq z_2^2 + \frac{1}{4}\mu^2$ ,  $b_4 z_4(x_{3,c} - \alpha_3) \leq \frac{b_4^2}{4}\mu^2 + z_4^2$ ,  $-\tilde{\theta} \hat{\theta} \leq -\frac{\tilde{\theta}^2}{2} + \frac{\theta^2}{2}$ , and (17) can be rewritten in the following inequality

$$\begin{aligned} \dot{V} \leq & -(k_1 - 1)z_1^2 - (k_2 - 1)z_2^2 - k_3 z_3^2 - (k_4 - 1)z_4^2 - k_5 z_5^2 - \frac{m_1 \tilde{\theta}^2}{2r_1} + \frac{1}{2}\varepsilon_1^2 d^2 \\ & + \frac{m_1 \theta^2}{2r_1} + \frac{1}{2}l_2^2 + \frac{1}{2}\varepsilon_2^2 + \frac{1}{2}l_3^2 + \frac{1}{2}\varepsilon_3^2 + \frac{1}{2}l_5^2 + \frac{1}{2}\varepsilon_5^2 + \frac{1}{4}\mu^2 (2 + b_4^2) \\ \leq & -aV + b \end{aligned} \quad (18)$$

where  $a = \min \{2(k_1 - 1)/J, 2(k_2 - 1), 2k_3, 2(k_4 - 1), 2k_5, m_1\}$  and  $b = \frac{1}{2}l_2^2 + \frac{1}{2}\varepsilon_2^2 + \frac{1}{2}l_3^2 + \frac{1}{2}\varepsilon_3^2 + \frac{1}{2}l_5^2 + \frac{1}{2}\varepsilon_5^2 + \frac{1}{2}\varepsilon_1^2 d^2 + \frac{m_1 \theta^2}{2r_1} + \frac{1}{4}\mu^2 (2 + b_4^2)$ . Then, (18) implies that

$$V(t) \leq \left( V(t_0) - \frac{b}{a} \right) e^{-a(t-t_0)} + \frac{b}{a} \leq V(t_0) + \frac{b}{a}, \quad \forall t \geq t_0 \quad (19)$$

All  $z_i$  ( $i = 1, 2, 3, 4$ ) and  $\tilde{\theta}$  belong to the compact set  $\Omega = \left\{ \left( z_i, \tilde{\theta} \right) \mid V \leq V(t_0) + \frac{b}{a}, \forall t \geq t_0 \right\}$ . Namely, all the signals in the closed-loop system are bounded. Especially, from (19) we can get  $\lim_{t \rightarrow \infty} z_1^2 \leq \frac{2b}{a}$ . By the definitions of  $a$  and  $b$ , it is proved that to get a small tracking error we can take  $r_i$  large but  $l_i$  and  $\varepsilon_i$  small enough after giving the parameters  $k_i$  and  $m_i$ .

**Remark 3.1.** *By comparing the command filtered based adaptive fuzzy controllers  $u_q$  and  $u_d$  with the classical backstepping controllers (35) and (39) given in [8], it can be seen that the classical controllers (35) and (39) are much more complicated than the proposed fuzzy controllers  $u_q$  and  $u_d$  in this paper. The numbers of terms (35) and (39) are much larger. This drawback was called explosion of complexity in [9].*

**4. Simulation Results.** In order to illustrate the effectiveness of the proposed results, the simulation is run for the induction motors with the parameters:  $J = 0.0586\text{Kgm}^2$ ,  $R_s = 0.1\Omega$ ,  $R_r = 0.15\Omega$ ,  $L_s = L_r = 0.0699\text{H}$ ,  $L_m = 0.068\text{H}$ ,  $n_p = 1$ . The simulation is carried out under the zero initial conditions the same as [10]. The reference signals are taken as  $x_{1d} = 0.5 \sin t + 0.3 \sin (0.5t)$  and  $x_{4d} = 1$ .  $T_L$  is chosen as  $T_L = \begin{cases} 0.5, & 0 \leq t \leq 5, \\ 1.0, & t \geq 5. \end{cases}$

The RBF NNs are chosen in the following way. The NNs  $\phi_2^T P_2(Z)$ ,  $\phi_3^T P_3(Z)$  and  $\phi_5^T P_5(Z)$  contain eleven nodes with centers spaced evenly in the interval  $[-9, 9]$  and widths being equal to 2, respectively. The proposed adaptive neural controllers are used to control the induction motor. The control parameters are chosen as:  $k_1 = 200$ ,  $k_2 = 100$ ,  $k_3 = 100$ ,  $k_4 = 100$ ,  $k_5 = 200$ ,  $r_1 = 0.05$ ,  $m_1 = 0.5$ ,  $l_2 = l_3 = l_5 = 0.5$ ,  $\zeta = 0.5$ ,  $\omega_n = 500$ .

Figure 1 displays the reference signals  $x_1$  and  $x_{1d}$  and Figure 2 shows the reference signals  $x_4$  and  $x_{4d}$ . It can be observed from Figure 1 and Figure 2 that the system output can track the given reference signals well and the tracking errors can converge to a small neighborhood of the origin. Figure 3 and Figure 4 demonstrate the trajectories of  $u_q$  and  $u_d$ . It can be observed that the controllers are bounded into a certain area that make them achieved in real applications. We can see a load torque disturbance appearing at

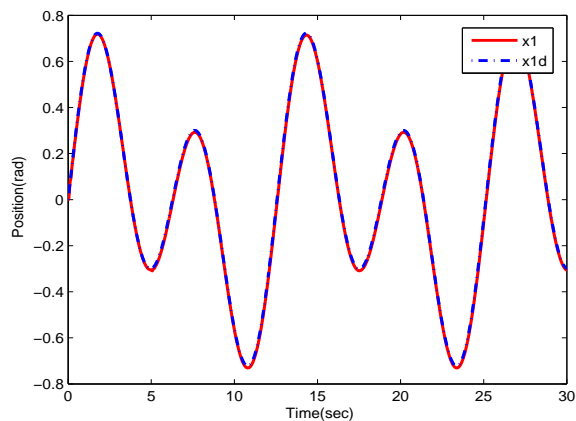


FIGURE 1. Trajectories of  $x_1$  and  $x_{1d}$

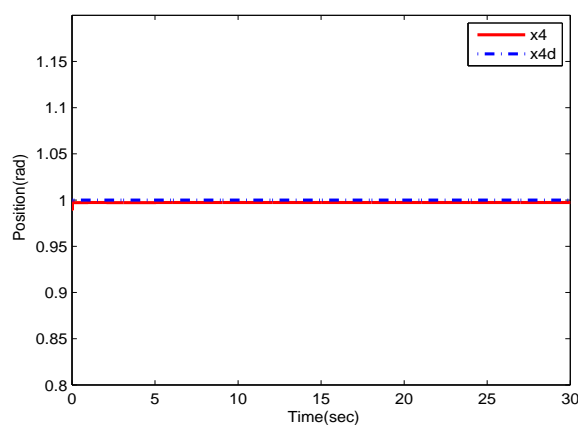


FIGURE 2. Trajectories of  $x_4$  and  $x_{4d}$

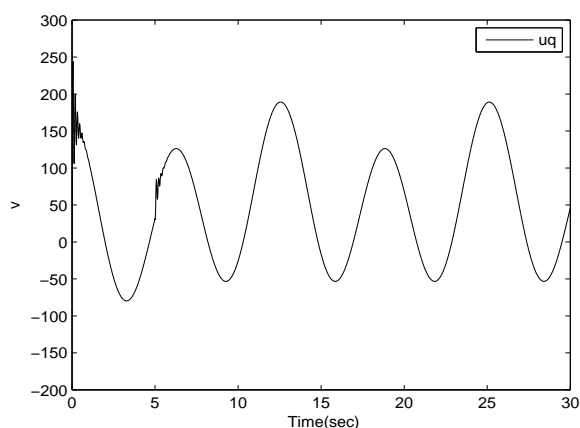


FIGURE 3. Trajectory of the control law  $u_q$

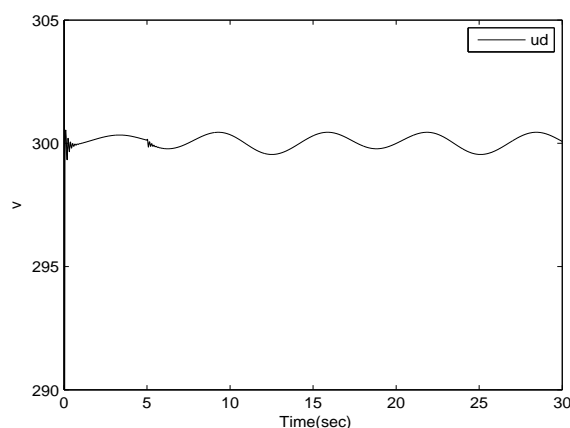


FIGURE 4. Trajectory of the control law  $u_d$

$t = 5s$  from Figure 3 and Figure 4. However, from the above simulation results, it is clearly shown that the proposed control method can track the reference signal quite well even under parameter uncertainties and load torque disturbance.

**5. Conclusions.** Neural network-based adaptive command filtered backstepping approach has been presented for the position tracking control of induction motors in this paper. This method can overcome the problem of “explosion of complexity” inherent in the traditional backstepping design. The designed controllers guarantee the tracking error can converge to a small neighborhood of the origin. Simulation results testify its effectiveness in the IM drive systems. In the future work, we will focus on the proposed control algorithm applied to the realistic industrial applications.

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